



COURSE (MODULE) DESCRIPTION

| Course title | Code |
|--------------------|------|
| Statistical Theory | |

| Staff | Department |
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| Coordinator: Dr Povilas Lastauskas and Ovidijus Stauskas (Lund University, Sweden) Other(s): Dr Ieva Mikaliūnaitė | Faculty of Economics and Business Administration |

| Study cycle | Course type |
|--------------------|-------------|
| First (Bachelor's) | Compulsory |

| Form of implementation | Period of implementation | Language of instruction |
|-------------------------|--------------------------|-------------------------|
| Face-to-face and online | Semester 1 and 2 | English |

| Requirements for student | |
|--------------------------|--|
| Prerequisites: | Additional requirements (if any): |

| Number of ECTS credits | Student's workload | Contact hours | Individual work |
|------------------------|--------------------|---------------|-----------------|
| 10 | 260 | 72 | 188 |

| Purpose of the course and competences developed |
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| This course aims to provide theoretical knowledge of both the frequentist and the Bayesian approaches to statistics, useful for the statistical analysis of economic, financial, and social problems. |

| Learning outcomes (learning outcomes of the programme) | Teaching methods | Assessment methods |
|--|---|-----------------------------------|
| To be in possession of a good grasp of the elementary tools of descriptive statistics; should understand elementary principles of probability and statistical theory; should be competent in applying basic methods of statistical inference as well as Bayesian approach to statistics. (1.2) | Lectures and lecture notes, tutorials. | Written examination and homework. |
| Find relevant data, evaluate its quality, conduct statistical analysis using modern software packages and prepare a final report using scientific typesetting tools. (3.4) | Lectures and lecture notes, tutorials, labs, and independent statistical project. | |
| Expand own understanding, knowledge and skills working on problem sets independently (5.1) | Individual homework assignments. | |
| The ability to work in teams delivering an empirical project (4.1) | Group homework assignments. | |

| Course themes | Contact / Individual work: time and assignments | | | | | | | | Assignments due date |
|--|---|-----------|----------|-------------------|-----------------|----------|---------------|-----------------|---|
| | Lectures | Tutorials | Seminars | Practical classes | Laboratory work | Practice | Contact hours | Individual work | |
| FALL semester (Statistical Theory I) | | | | | | | | | |
| Review of Statistical Science | 2 | | | | | | 2 | 5 | |
| Descriptive Statistics | 2 | | | | | | 2 | 5 | |
| Probability: events, outcomes and sample space; Venn diagrams; unions, intersections and complements; simple combinatorial formulae for sampling with and without replacement; random variables | 4 | 2 | | | | | 6 | 10 | |
| Probability distributions: univariate discrete and continuous distributions; probability mass functions; cumulative distribution functions and probability density functions; expectations, variances and higher moments; Bernoulli trials and the Binomial distribution; Uniform and Normal distributions; Chi-squared, t and F distributions | 6 | 2 | | | | | 8 | 20 | Problem Set 1 Emphasis on combinatorial basics of probability, probability distributions and densities. MM chapters 2-3, Appendices B and C. LM chapter 2. |
| Sample statistics: the concept of an estimator; unbiasedness and efficiency; sampling distributions, Law of Large Numbers and Central Limit Theorem | 6 | | | | | | 6 | 20 | |
| Estimation and Inference: point and confidence interval estimation and hypothesis testing; null and alternative hypotheses; critical regions; one-tailed and two-tailed tests; Type I and Type II errors; power functions | 4 | 2 | | | | | 6 | 15 | Problem Set 2 Group Project |
| Bivariate Regression: ordinary least squares, conditional expectations function, tests of significance, sampling distributions of regression coefficients | 6 | 2 | | | | | 8 | 20 | Problem Set 3 Work on hypothesis testing and estimation. MM chapters 12-13, 14.1-14.4. LM chapters 5-7. Time permitting: Tutorial on running simple regressions, interpreting results, conducting hypothesis testing. |
| SPRING semester (Statistical Theory II) | | | | | | | | | |
| Review of Probability: axioms, conditional probability, random variables, mean, variance. | 3 | 2 | | | | | 6 | 20 | Tutorial on R and its use for Bayesian |

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|--|-----------|-----------|--|--|--|--|-----------|------------|--|
| | | | | | | | | | inference; Individual homework 1 |
| Discrete and Continuous random variables: Bernoulli, Binomial, Poisson, Exponential, Gamma, Beta, Gaussian. Their properties, means, variances. | 3 | 2 | | | | | 6 | 20 | Individual homework 2 |
| Bayesian Inference for Discrete Random variables: likelihood, prior, conjugacy, posterior and posterior predictive distributions. | 6 | 2 | | | | | 4 | 10 | Individual homework 3; |
| Bayesian Inference for Continuous Random Variables. Gaussian Model and Bayesian Linear regression. | 6 | 2 | | | | | 12 | 25 | Individual homework 4,5 |
| Differences between Bayesian and Frequentist views – the big picture. | 6 | 2 | | | | | 6 | 18 | R-programming project and Individual homework 6 |
| Total | 54 | 18 | | | | | 72 | 188 | |

| Assessment strategy | Share in % | Time of assessment | Assessment criteria |
|--|---------------|-------------------------------------|--|
| Fall semester (Statistical Theory I) | | | |
| Written exam | 50 | End of fall semester | The final exam will consist of open and mathematical questions in which students have to show their knowledge and analytical capabilities, and shorter questions testing knowledge of main concepts and statistical ideas. |
| Problem sets | 30 | Throughout semester | There will be three problem sets, which will involve problem solving and data manipulation exercises. Only one randomly picked problem set per student will be graded. However, to get a grade, all three problem sets must be submitted. All problem sets will be returned at the same time, after the last one is being covered in classes. |
| Group project | 20 | Second half of the fall semester | Presentation in class of the real-world data exercise, answering questions, and demonstrating knowledge of main statistical concepts. |
| Spring semester (Statistical Theory II) | | | |

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|---------------------|----|-------------------|---|
| Written exam | 70 | End of semester | Exam questions include all topics covered in the course lectures and discussions. It is exercises based and is worth of 10 points. Each question is evaluated by 1 point using the evaluation criteria below: -1 point (excellent) evaluates the answer, giving a detailed and clear answer to a question based not only on lecture material but also on its own, substantiated reasoning. -The 0.5 point (well) evaluates the answer in detail, but not very accurately. -A score of 0.25 (weak) is considered the answer to be vague or incomplete, with several major errors. -0 points (unsatisfactory) no answer or it's completely wrong. |
| Programming project | 30 | During the course | The project evaluates students' skills in using R-program for data analysis with 3 questions. Each question is evaluated by the following criteria: correct answers, clear and readable codes, and simplicity. |

| Author | Published in | Title | Issue No. or Volume | Publishing house or Internet site |
|--|--------------|---|---------------------|--|
| Required reading | | | | |
| Lecture notes and slides as well as online resources will be made available to all students. Selected chapters from LM, MM and Bolstad are compulsory. | | | | |
| R J Larsen and M L Marx (Referred to as LM) | 2011 | An Introduction to Mathematical Statistics and its Applications | 5th Edition | Pearson |
| I Miller and M Miller (Referred to as MM) | 2012 | John E. Freund's Mathematical Statistics with Applications | 8th Edition | Pearson |
| Contributors | 2013 | OpenStax Intro Statistics | | Introductory Statistics - OpenStax |

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| D. Diez, M. Cetinkaya-Rundel, C. Barr (Editors) | 2019 | Open Intro Statistics | 4 th Edition | OpenIntro Statistics |
| William M. Bolstad and James M. Curran | 2017 | Introduction to Bayesian Statistics (3 rd edition) | | Wiley |
| Supplementary reading (text books) | | | | |
| James V Stone | 2013 | Bayes' Rule: A tutorial Introduction to Bayesian Analysis | | Sebtel Press |
| D.S.Sivia and J.Skilling | 2006 | Data Analysis: A Bayesian Tutorial | | Oxford University Press |

